

> *with(plots)*
[*animate, animate3d, animatecurve, arrow, changecoords, complexplot, complexplot3d, conformal, conformal3d, contourplot, contourplot3d, coordplot, coordplot3d, densityplot, display, dualaxisplot, fieldplot, fieldplot3d, gradplot, gradplot3d, implicitplot, implicitplot3d, inequal, interactive, interactiveparams, intersectplot, listcontplot, listcontplot3d, listdensityplot, listplot, listplot3d, loglogplot, logplot, matrixplot, multiple, odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot, polygonplot, polygonplot3d, polyhedra_supported, polyhedraplot, rootlocus, semilogplot, setcolors, setoptions, setoptions3d, spacecurve, sparsematrixplot, surfdata, textplot, textplot3d, tubeplot*]

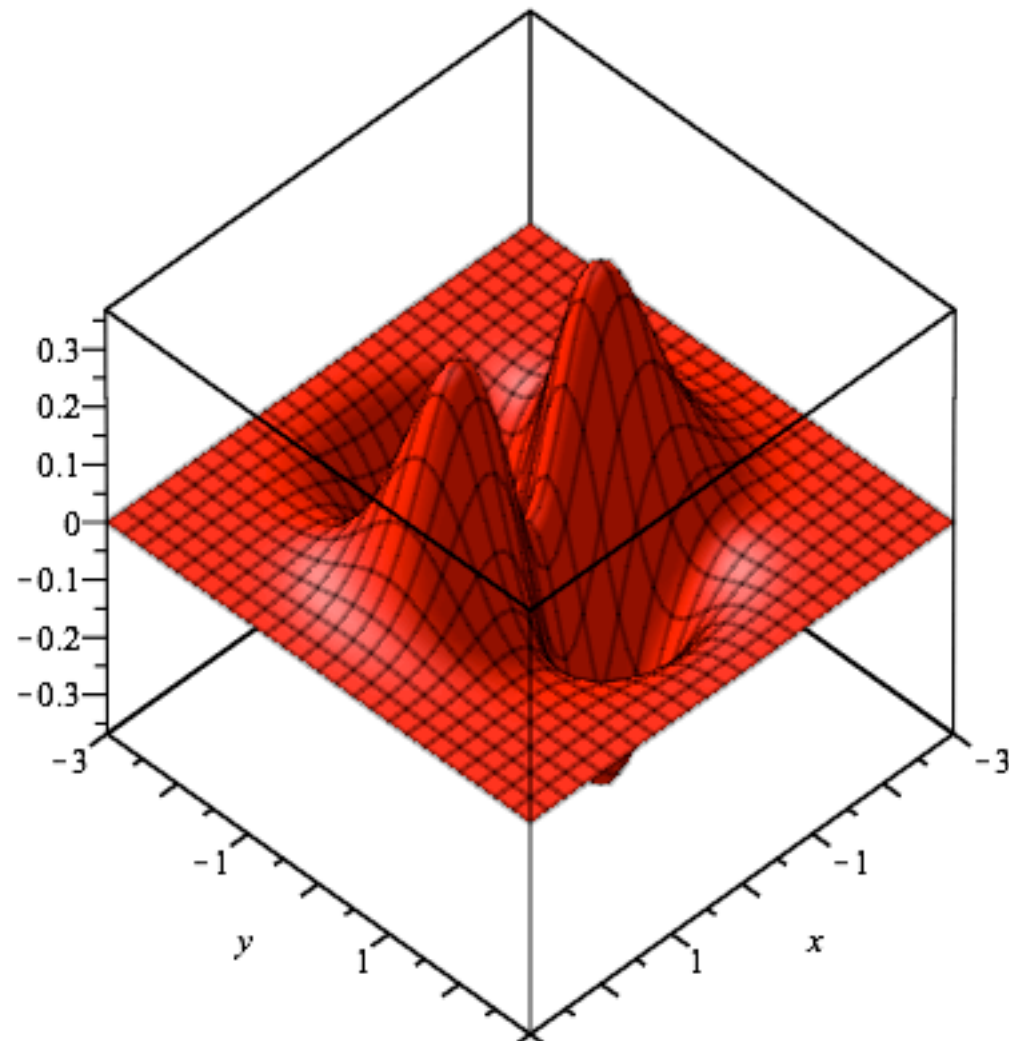
(1

Oppgave 10.1.14

a)

(i)

> *plot3d(($x^2 - y^2$) · exp(- $x^2 - y^2$), x = -3 .. 3, y = -3 .. 3, axes = boxed, color = red, labels = [x, y, z])*



(ii)

Av figuren ser det lurt ut å velge nivåkurver der $f(x, y) = 0, \pm 0.1, \pm 0.2, \pm 0.3$.

For å slippe å skrive opp uttrykket for funksjonen 7 ganger, definerer vi først funksjonen $f(x, y)$:

> $f := (x, y) \rightarrow (x^2 - y^2) \cdot \exp(-x^2 - y^2)$

$$f := (x, y) \rightarrow (x^2 - y^2) e^{-x^2 - y^2}$$

(2)

> $P1 := \text{implicitplot}(f(x, y) = 0.3, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{red}, \text{numpoints} = 10000)$

$P1 := \text{PLOT}(\dots)$

(3)

> $P2 := \text{implicitplot}(f(x, y) = 0.2, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{orange}, \text{numpoints} = 10000)$

$P2 := \text{PLOT}(\dots)$

(4)

> $P3 := \text{implicitplot}(f(x, y) = 0.1, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{yellow}, \text{numpoints} = 10000)$

$P3 := \text{PLOT}(\dots)$

(5)

> $P4 := \text{implicitplot}(f(x, y) = 0, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{green}, \text{numpoints} = 10000)$

$P4 := \text{PLOT}(\dots)$

(6)

> $P5 := \text{implicitplot}(f(x, y) = -0.1, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{blue}, \text{numpoints} = 10000)$

$P5 := \text{PLOT}(\dots)$

(7)

> $P6 := \text{implicitplot}(f(x, y) = -0.2, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{magenta}, \text{numpoints} = 10000)$

$P6 := \text{PLOT}(\dots)$

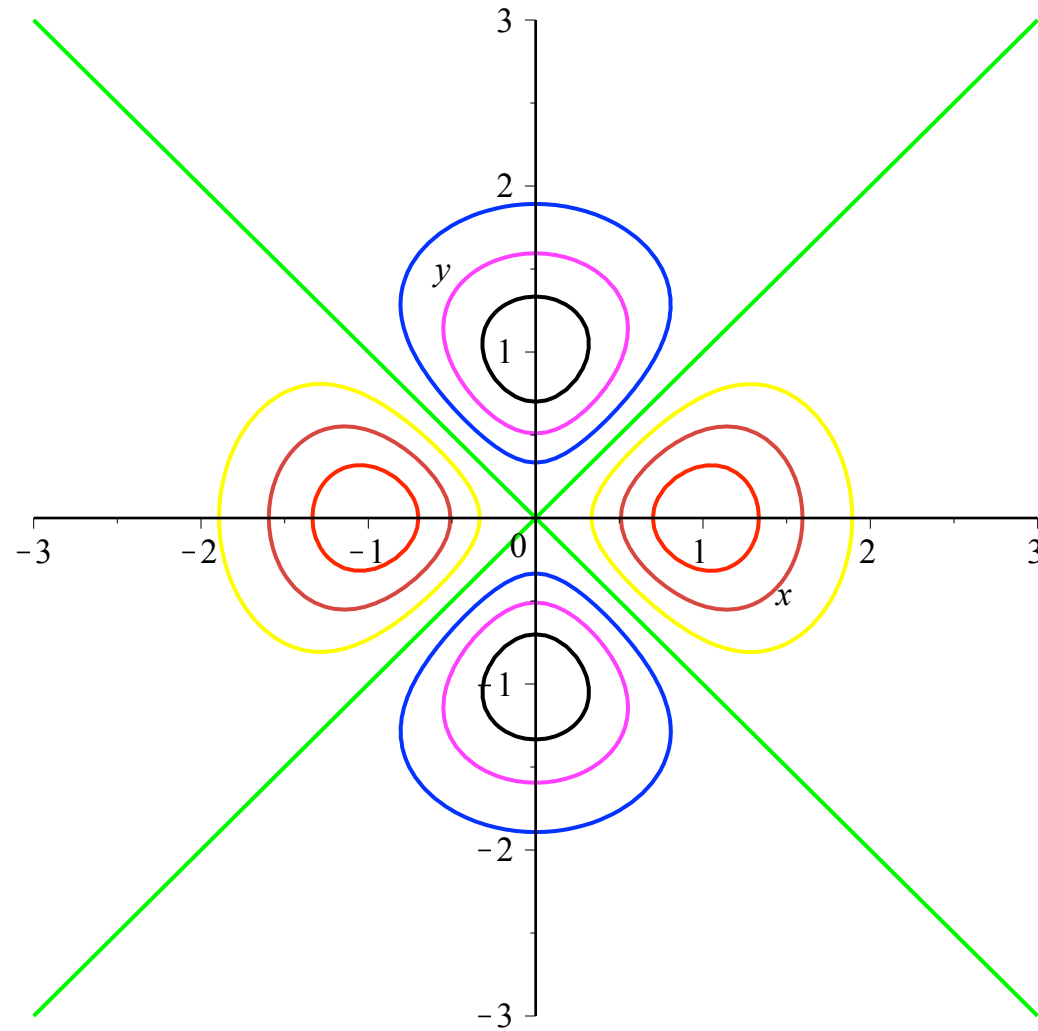
(8)

> $P7 := \text{implicitplot}(f(x, y) = -0.3, x = -3 \dots 3, y = -3 \dots 3, \text{color} = \text{black}, \text{numpoints} = 10000)$

$P7 := \text{PLOT}(\dots)$

(9)

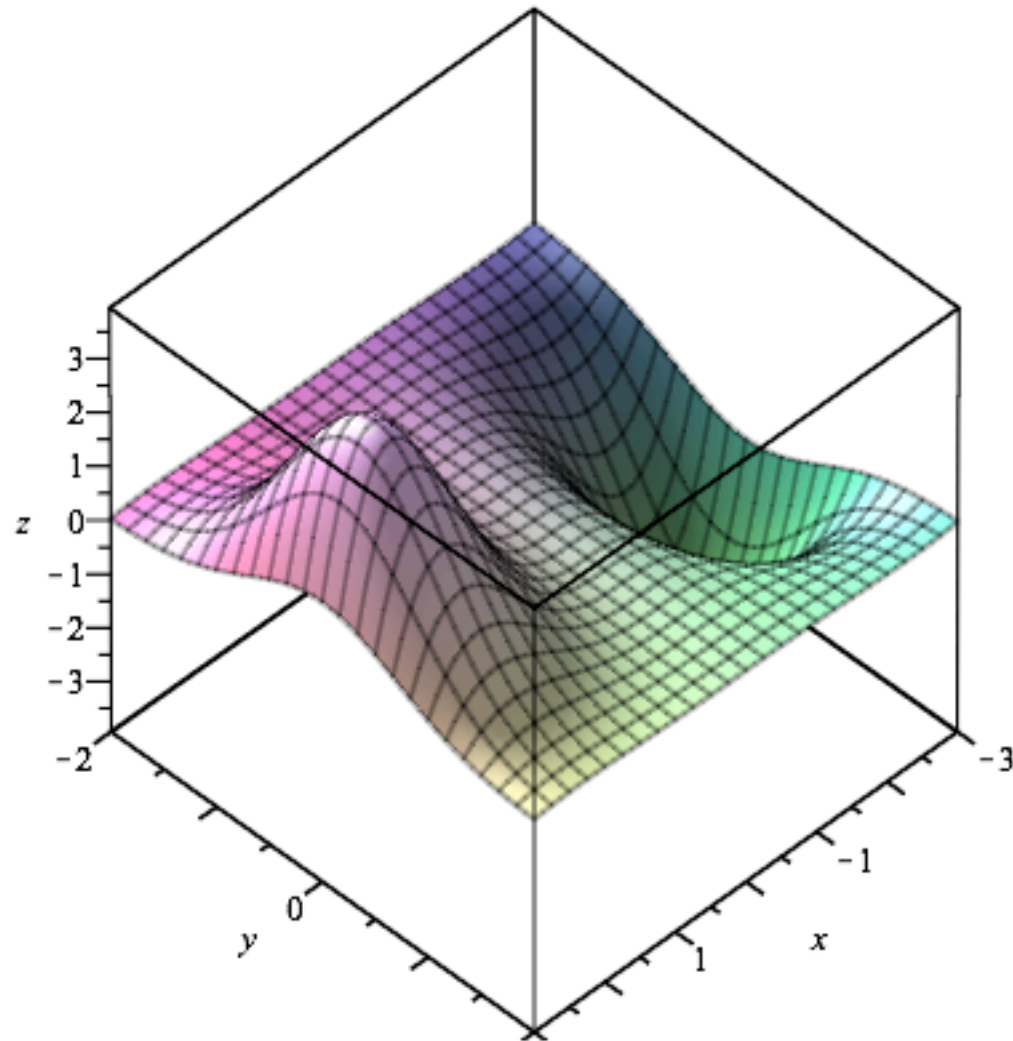
> $\text{display}(P1, P2, P3, P4, P5, P6, P7)$



d)

(i)

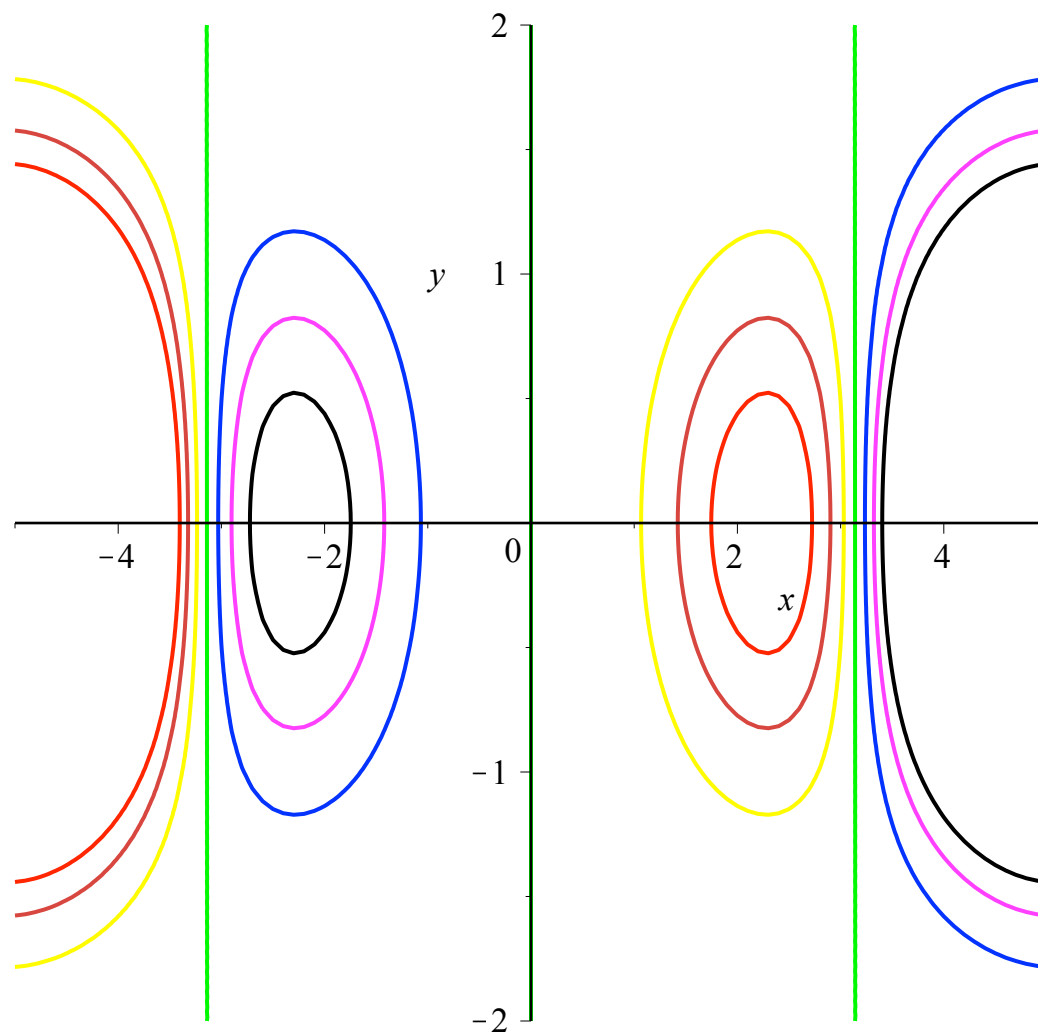
> `plot3d(x^2*exp(-y^2)*sin(x), x=-3..3, y=-2..2, axes = boxed, labels = [x, y, z])`



(ii)

> $P1 := \text{implicitplot}(x^2 \cdot \exp(-y^2) \cdot \sin(x) = 3, x = -5..5, y = -2..2, \text{gridrefine} = 2, \text{color} = \text{red})$
 $P1 := \text{PLOT}(\dots)$

<pre>> P2 := implicitplot(x^2·exp(-y^2)·sin(x) = 2, x = -5..5, y = -2..2, gridrefine = 2, color = orange) P2 := PLOT(...)</pre>	(11)
<pre>> P3 := implicitplot(x^2·exp(-y^2)·sin(x) = 1, x = -5..5, y = -2..2, gridrefine = 2, color = yellow) P3 := PLOT(...)</pre>	(12)
<pre>> P4 := implicitplot(x^2·exp(-y^2)·sin(x) = 0, x = -5..5, y = -2..2, gridrefine = 2, color = green) P4 := PLOT(...)</pre>	(13)
<pre>> P5 := implicitplot(x^2·exp(-y^2)·sin(x) = -1, x = -5..5, y = -2..2, gridrefine = 2, color = blue) P5 := PLOT(...)</pre>	(14)
<pre>> P6 := implicitplot(x^2·exp(-y^2)·sin(x) = -2, x = -5..5, y = -2..2, gridrefine = 2, color = magenta) P6 := PLOT(...)</pre>	(15)
<pre>> P7 := implicitplot(x^2·exp(-y^2)·sin(x) = -3, x = -5..5, y = -2..2, gridrefine = 2, color = black) P7 := PLOT(...)</pre>	(16)
<pre>> display(P1, P2, P3, P4, P5, P6, P7)</pre>	



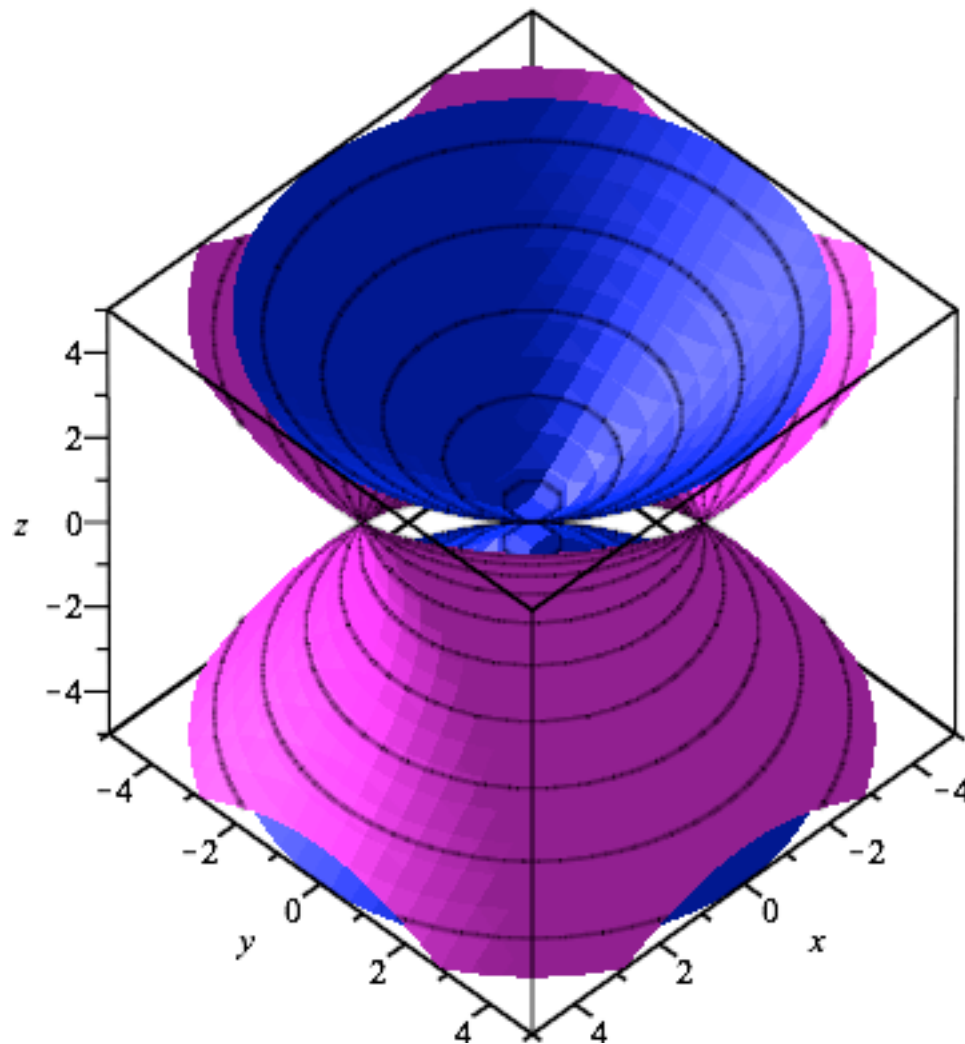
Oppgave 10.1.15

a)

```
> P1 := implicitplot3d( $x^2 + y^2 - z^2 = 0$ ,  $x = -5 \dots 5$ ,  $y = -5 \dots 5$ ,  $z = -5 \dots 5$ , color = blue, numpoints = 10000, style = surfacecontour)
P1 := PLOT3D(...) (17)
```

```
> P2 := implicitplot3d( $x^2 + y^2 - z^2 = 8$ ,  $x = -5 \dots 5$ ,  $y = -5 \dots 5$ ,  $z = -5 \dots 5$ , color = magenta, numpoints = 10000, style = surfacecontour)
P2 := PLOT3D(...) (18)
```

```
> display(P1, P2)
```



Vi ser figuren best ved å dreie litt på den. Gjør det!

P1 er egentlig en dobbel kjegle, men Maple mangler noen punkter nær origo der dobbelkjeglen er smalest. (Slikt kan skje, men det hjelper å be om flere punkter.)

P2 er en enkappet hyperboloide. Det dumme er at P2 skygger for P1.

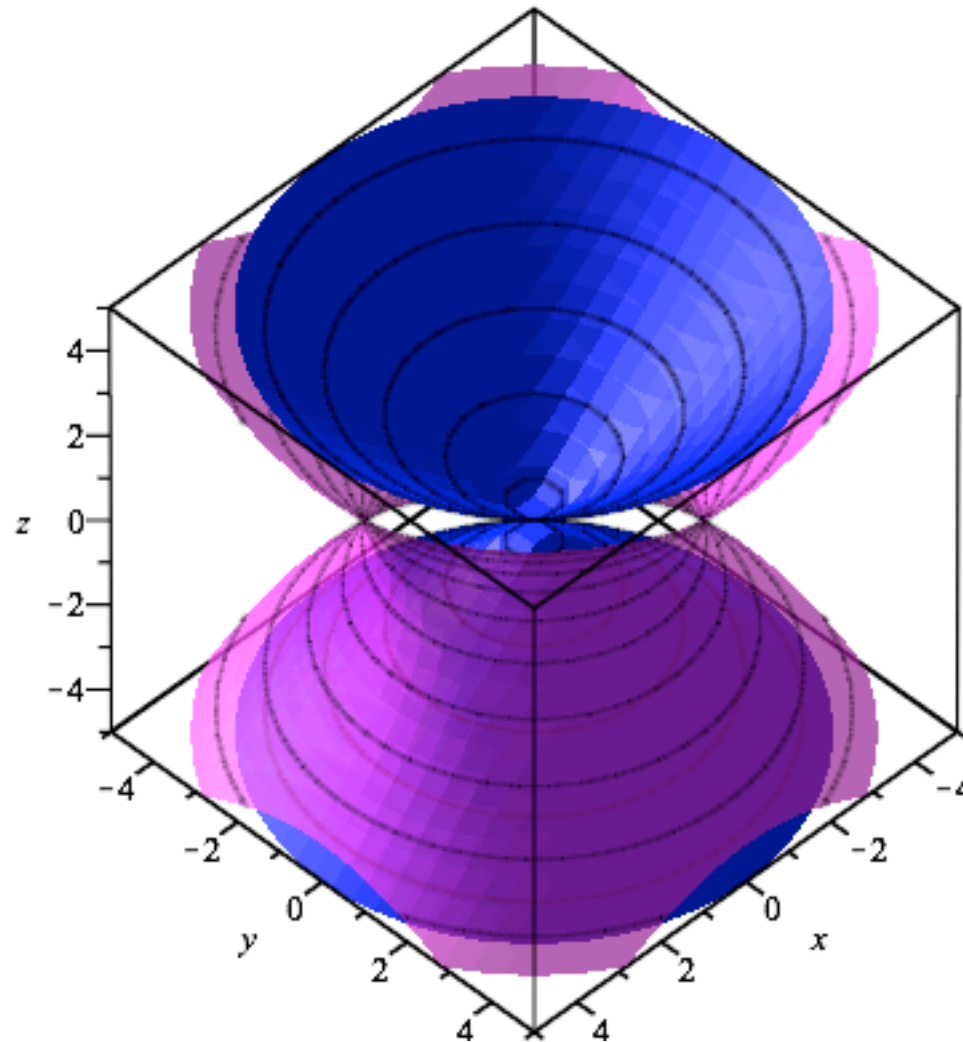
Vi kan gjøre P2 litt gjennomsiktig:

```
> P2 := implicitplot3d( $x^2 + y^2 - z^2 = 8$ ,  $x = -5 \dots 5$ ,  $y = -5 \dots 5$ ,  $z = -5 \dots 5$ , color = magenta, numpoints = 10000, style = surfacecontour, transparency = 0.3)
```

```
P2 := PLOT3D(...)
```

(19

```
> display(P1, P2, axes = boxed, labels = [x, y, z])
```



Det ble kanskje litt bedre.

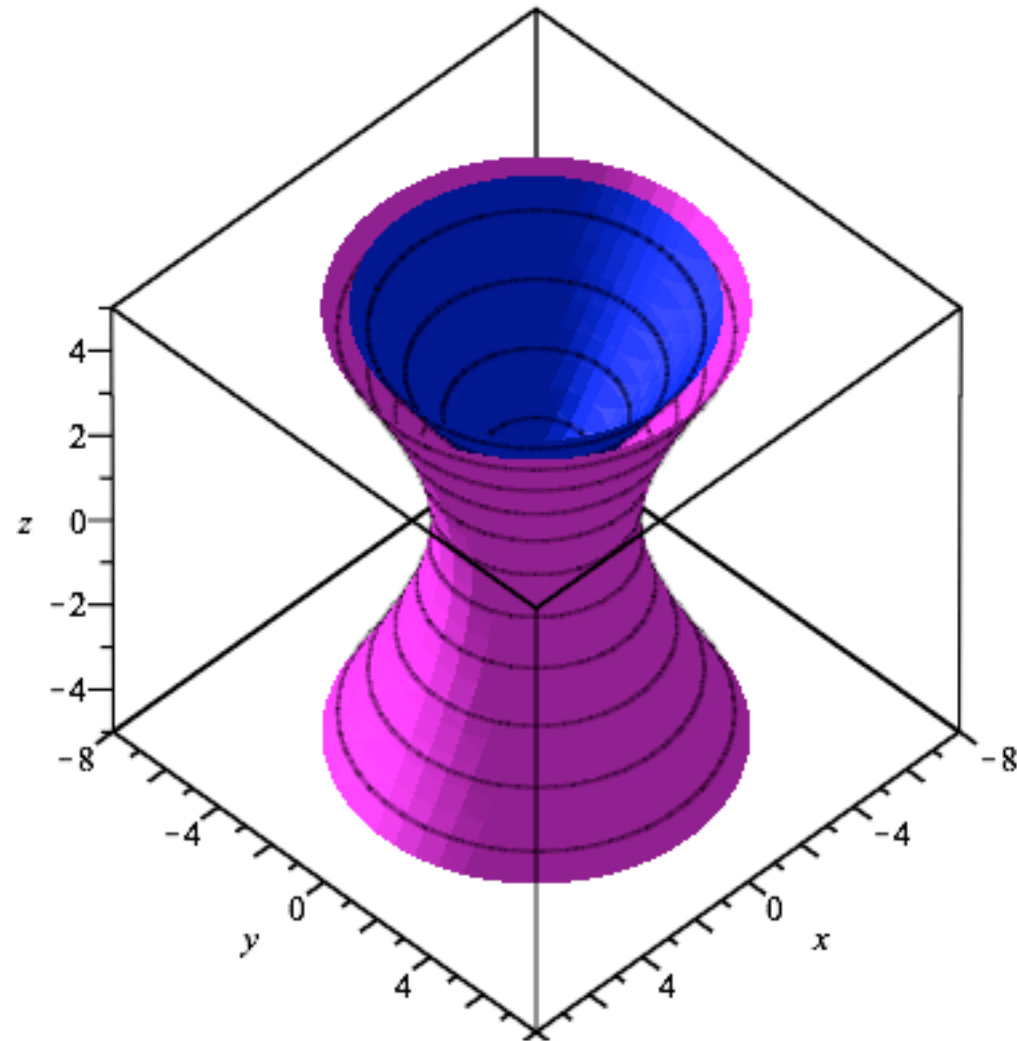
Men den røde flaten burde vel også ha vært kuttet av i en sirkel og ikke med et kvadrat.

```
> P2 := implicitplot3d( $x^2 + y^2 - z^2 = 8$ ,  $x = -8 .. 8$ ,  $y = -8 .. 8$ ,  $z = -5 .. 5$ , color = magenta, numpoints = 10000, style = surfacecontour)
```

```
P2 := PLOT3D(...)
```

(20

```
> display(P1, P2)
```



Ser du hvorfor denne forandringen i kommandoen fungerede?

>