

Vi henter inn Maples plottekommandoer og vectorCalculus-kommandoer like godt først som sist:

```
> with(plots)
[animate, animate3d, animatecurve, arrow, changecoords, complexplot, complexplot3d, conformal, conformal3d, contourplot,
contourplot3d, coordplot, coordplot3d, densityplot, display, dualaxisplot, fieldplot, fieldplot3d, gradplot, gradplot3d, implicitplot,
implicitplot3d, inequal, interactive, interactiveparams, intersectplot, listcontplot, listcontplot3d, listdensityplot, listplot, listplot3d,
loglogplot, logplot, matrixplot, multiple, odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot, polygonplot,
polygonplot3d, polyhedra_supported, polyhedraplot, rootlocus, semilogplot, setcolors, setoptions, setoptions3d, spacecurve,
sparsematrixplot, surfdata, textplot, textplot3d, tubeplot]
```

(1)

```
> with(VectorCalculus)
[&x, `*`, `+`, `^`, `.` , < , > , <|> , About, AddCoordinates, ArcLength, BasisFormat, Binormal, Compatibility, ConvertVector,
CrossProduct, Curl, Curvature, D, Del, DirectionalDiff, Divergence, DotProduct, Flux, GetCoordinateParameters,
GetCoordinates, GetNames, GetPVDDescription, GetRootPoint, GetSpace, Gradient, Hessian, IsPositionVector, IsRootedVector,
IsVectorField, Jacobian, Laplacian, LineInt, MapToBasis, Nabla, Norm, Normalize, PathInt, PlotPositionVector, PlotVector,
PositionVector, PrincipalNormal, RadiusOfCurvature, RootedVector, ScalarPotential, SetCoordinateParameters, SetCoordinates,
SpaceCurve, SurfaceInt, TNBFrame, Tangent, TangentLine, TangentPlane, TangentVector, Torsion, Vector, VectorField,
VectorPotential, VectorSpace, Wronskian, diff, eval, evalVF, int, limit, series]
```

(2)

### Ekstraoppgave 10.7.1

a)

```
> P1 := implicitplot(4 - x^2 - y^2 = 2, x = -2 .. 2, y = -2 .. 2, color = red)
P1 := PLOT(...)
```

(3)

```
> P2 := implicitplot(4 - x^2 - y^2 = 1, x = -2 .. 2, y = -2 .. 2, color = blue)
P2 := PLOT(...)
```

(4)

```
> P3 := implicitplot(4 - x^2 - y^2 = 3, x = -3 .. 3, y = -2 .. 2, color = magenta)
```

(5)

$$P3 := PLOT(\dots) \quad (5)$$

$$> G := \text{Gradient}(4 - x^2 - y^2, [x, y])$$

$$G := -2x\bar{e}_x - 2y\bar{e}_y \quad (6)$$

$$> Gs := \text{subs}(\{x = 1, y = 1\}, G)$$

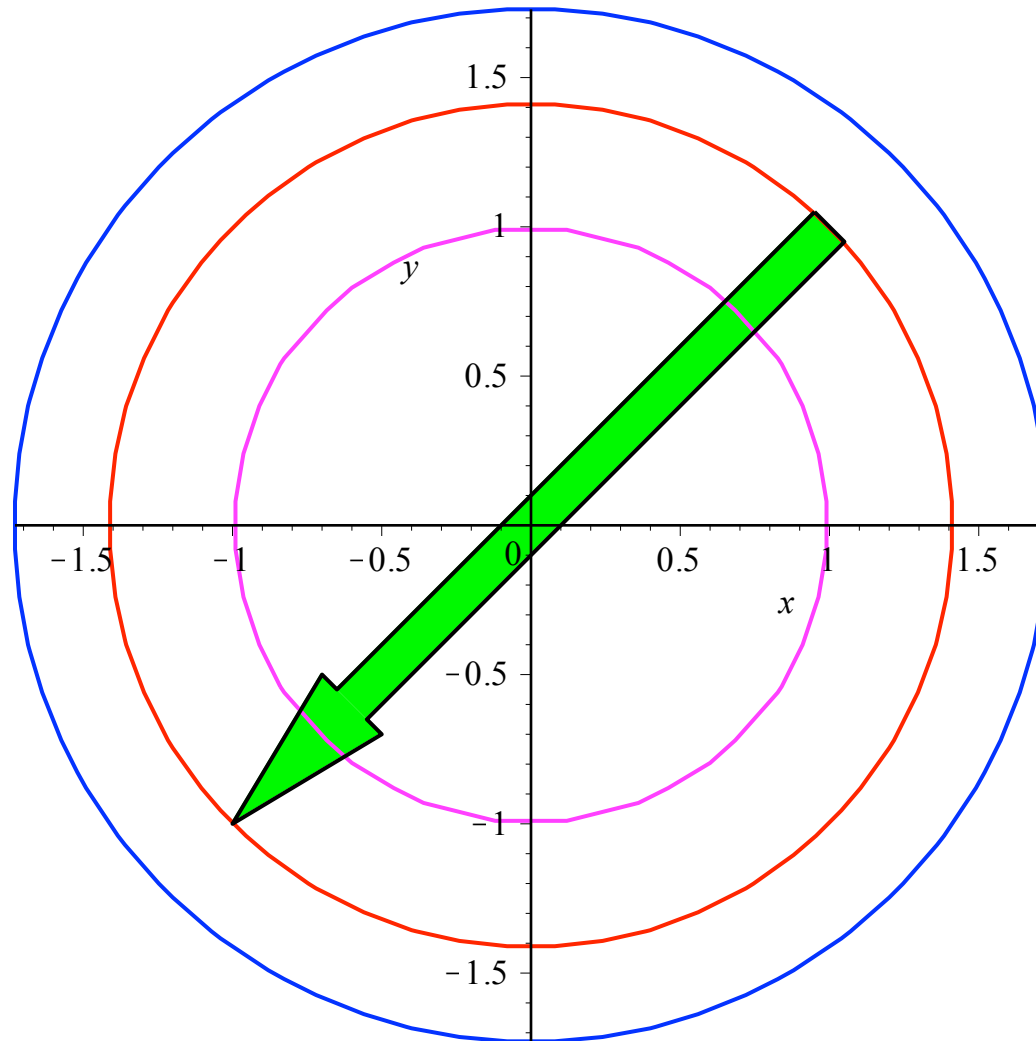
$$Gs := -2\bar{e}_x - 2\bar{e}_y \quad (7)$$

Kommandoen for å plotte en pil, er *arrow*. Vi skriver først startpunktet for pilen som en vektor (her  $\langle 1, 1 \rangle$ ). Deretter kommer selv pil-vektoren (her  $Gs$ )

$$> Q := \text{arrow}(\langle 1, 1 \rangle, Gs, \text{color} = \text{green})$$

$$Q := PLOT(\dots) \quad (8)$$

$$> \text{display}(P1, P2, P3, Q)$$

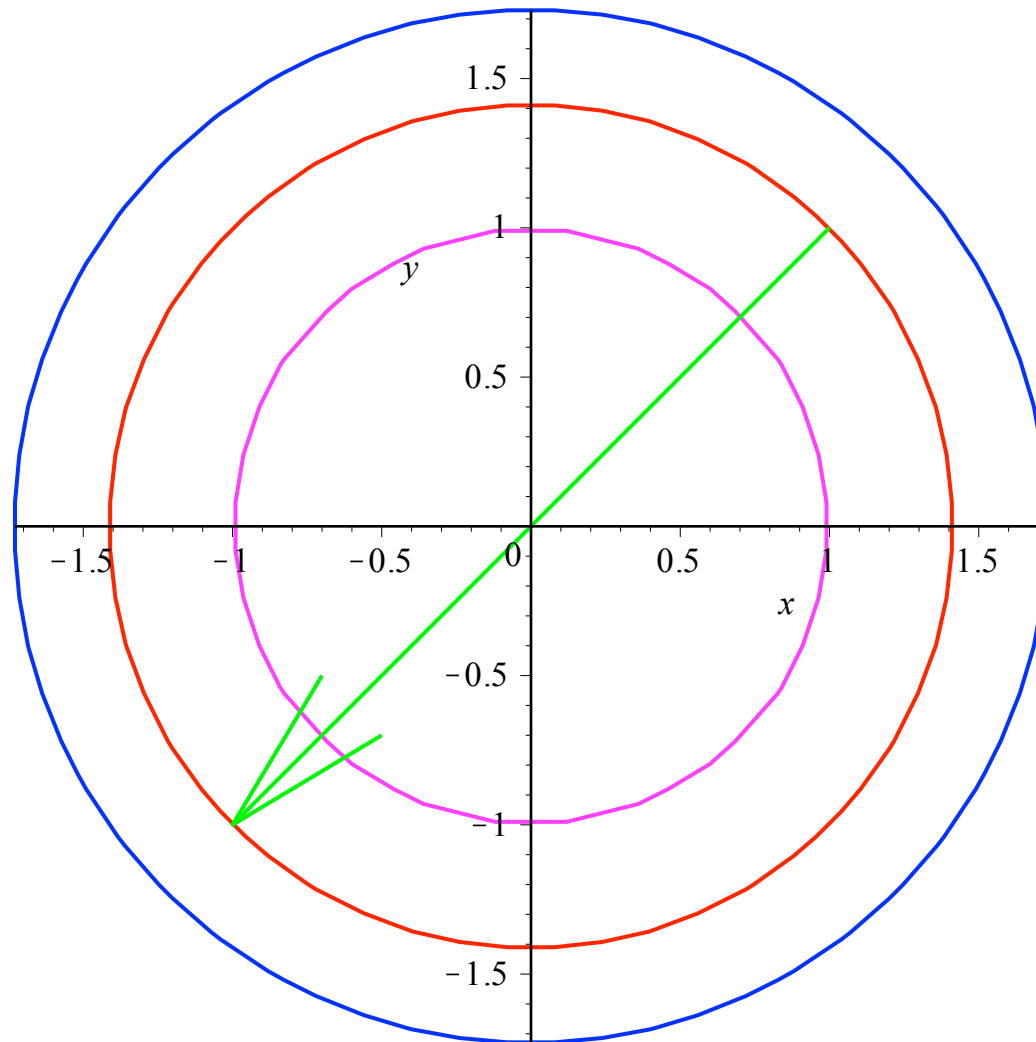


Denne vektoren ble ganske voldsom. Vi kan be om en tynnere vektor ved å skrive `shape = arrow`

> `Q := arrow(⟨1, 1⟩, Gs, color = green, shape = arrow)`

`Q := PLOT(...)`

> `display(P1, P2, P3, Q)`



Ser du at den grønne gradienvektoren står normal på nivåkurven gjennom punktet  $(1,1)$ , og peker i retning av voksende funksjonsverdi for  $F$  (den lilla nivåkurven går gjennom punkter med større funksjonsverdi enn den røde.)

b)

```
> P1 := implicitplot(exp(x)·sin(y) = 1, x=-5..5, y=-5..5, color = red, gridrefine = 2)
P1 := PLOT(...)
```

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```
> P2 := implicitplot(exp(x)·sin(y) = 2, x=-5..5, y=-5..5, color = blue, gridrefine = 2)
P2 := PLOT(...)
```

(11)

```
> P3 := implicitplot(exp(x)·sin(y) = -1, x=-5..5, y=-5..5, color = magenta, gridrefine = 2)
P3 := PLOT(...)
```

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```
> G := Gradient(exp(x)·sin(y), [x, y])
G := (ex sin(y))ex + (ex cos(y))ey
```

(13)

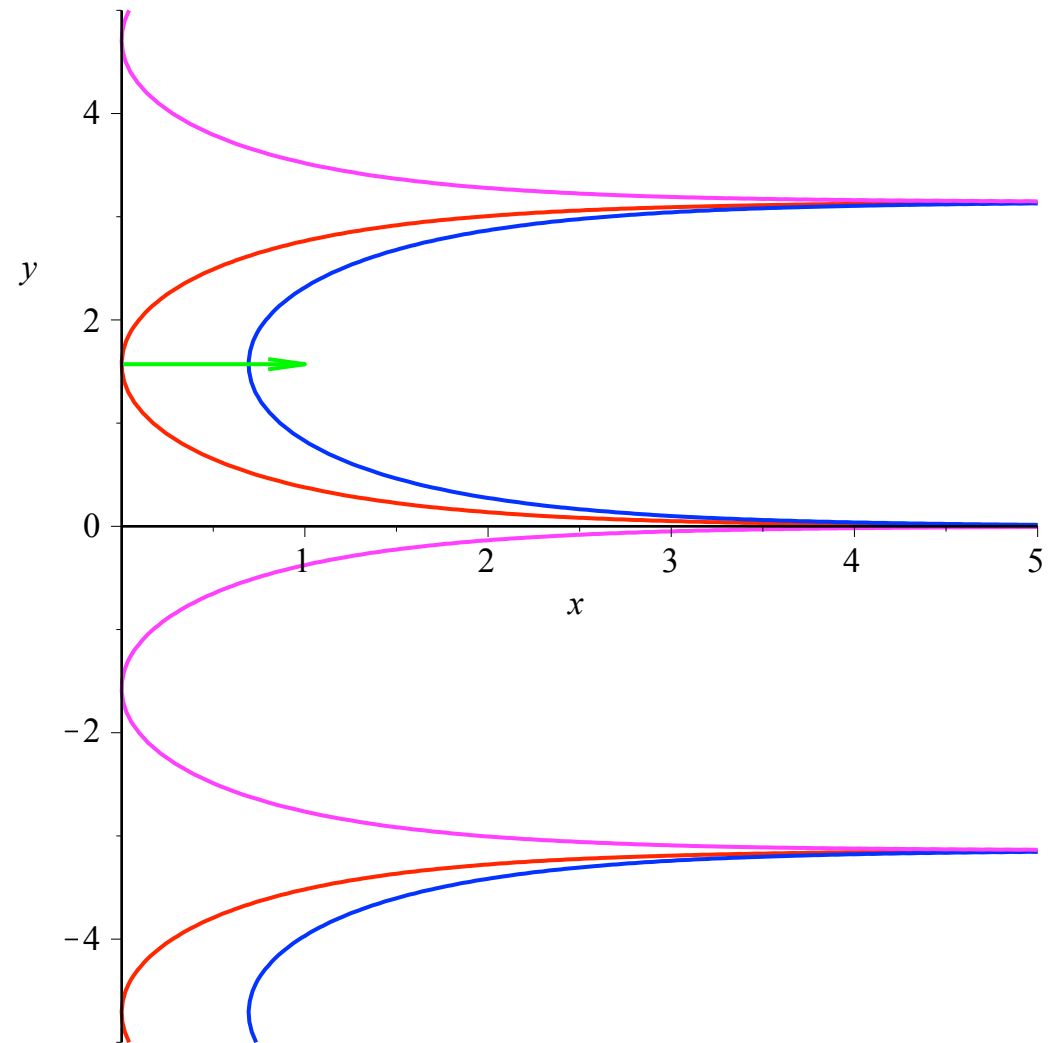
```
> Gs := subs( { x = 0, y = Pi/2 }, G )
Gs := ex
```

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```
> Q := arrow( < 0, Pi/2 >, Gs, color = green, shape = arrow )
Q := PLOT(...)
```

(15)

```
> display(P1, P2, P3, Q)
```



Ekstraoppgave 10.7.2.

a)

```
> P := implicitplot3d( $x^2 + y^2 + 2z^2 = 5$ ,  $x = -3..3$ ,  $y = -2..2$ ,  $z = -2..2$ , style = surfacecontour, color = yellow, numpoints = 10000)
P := PLOT3D(...)
```

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```
> G := Gradient( $x^2 + y^2 + 2z^2$ , [x, y, z])
G :=  $2x\bar{e}_x + 2y\bar{e}_y + 4z\bar{e}_z$ 
```

(17)

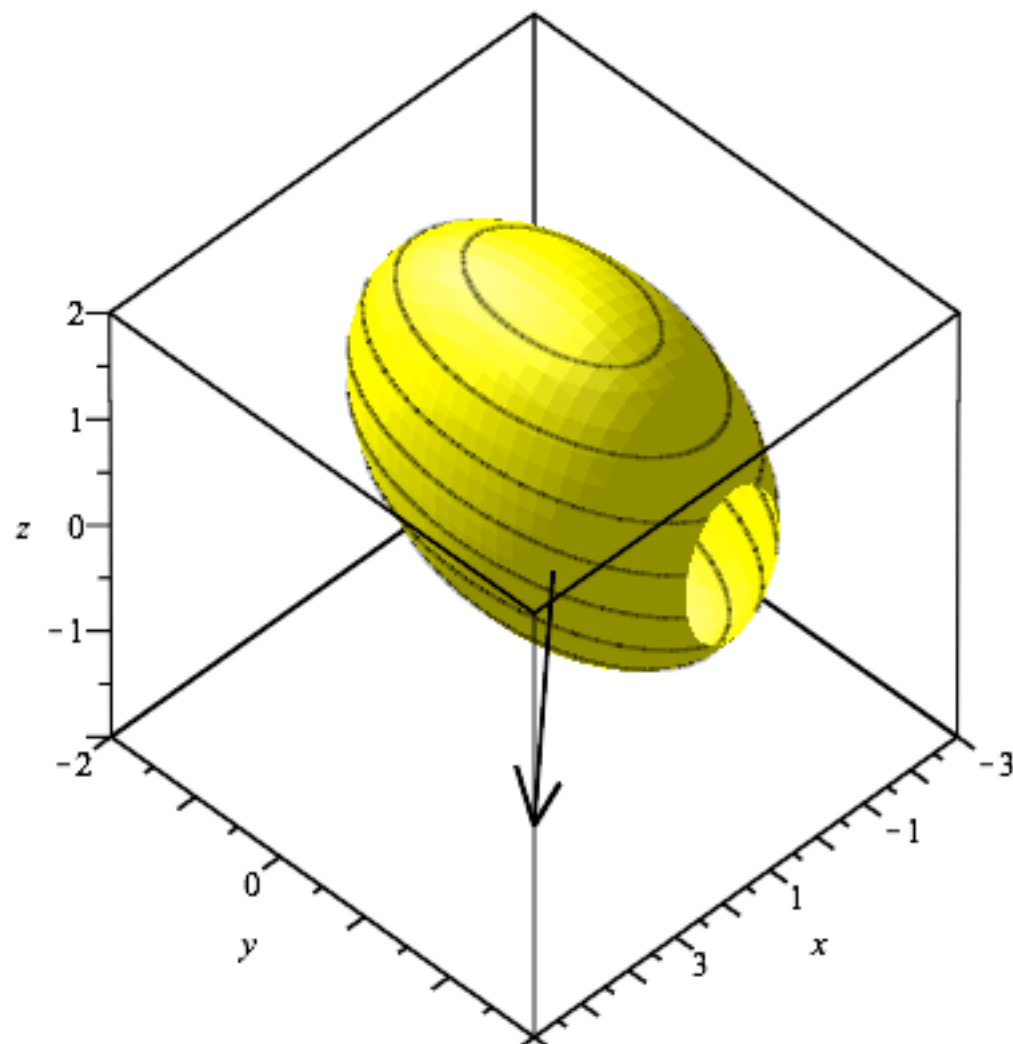
```
> Gs := subs({x = 2, y = 1, z = 0}, G)
Gs :=  $4\bar{e}_x + 2\bar{e}_y$ 
```

(18)

```
> Q := arrow(<2, 1, 0>, Gs, shape = arrow, color = black)
Q := PLOT3D(...)
```

(19)

```
> display(P, Q, axes = boxed)
```



Husk: du kan rotere bildet. Trykk først på bildet. Vil det ikke roteres, så trykk på rotasjonsknappen i den nederste kommandolinjen på toppen av arbeidsarket.

d)



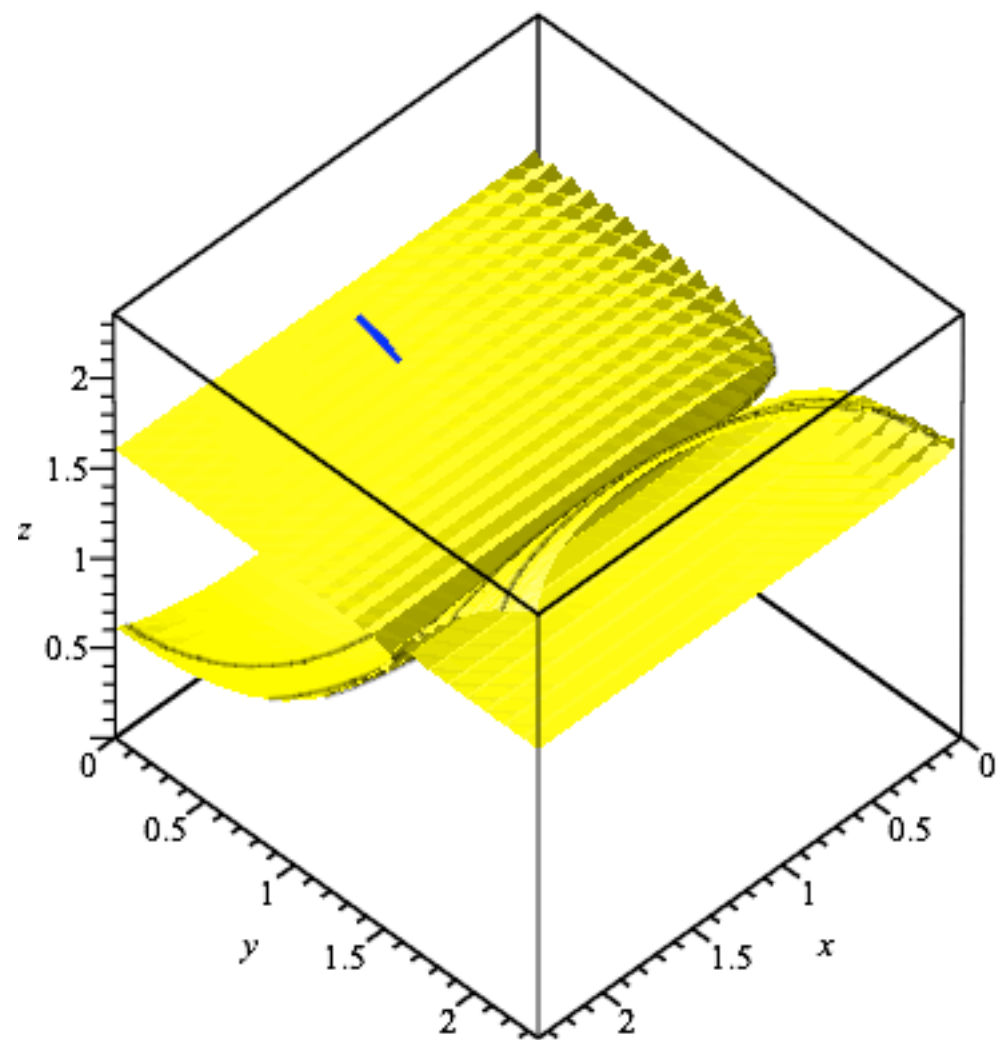
$$\begin{aligned} &> P := \text{implicitplot3d}\left(\sin(x) \cdot \cos(y) \cdot \tan(z) = \frac{1}{2}, x = 0 \dots \frac{3 \cdot \text{Pi}}{4}, y = -0 \dots \frac{3 \cdot \text{Pi}}{4}, z = 0 \dots \frac{3 \cdot \text{Pi}}{4}, \text{style} = \text{surfacecontour}, \text{color} = \text{yellow}, \right. \\ &\quad \left. \text{numpoints} = 10000\right) \\ &\quad P := \text{PLOT3D}(\dots) \end{aligned} \tag{20}$$

$$\begin{aligned} &> G := \text{Gradient}(\sin(x) \cdot \cos(y) \cdot \tan(z), [x, y, z]) \\ &\quad G := (\cos(x) \cos(y) \tan(z)) \bar{e}_x - \sin(x) \sin(y) \tan(z) \bar{e}_y + (\sin(x) \cos(y) (1 + \tan(z)^2)) \bar{e}_z \end{aligned} \tag{21}$$

$$\begin{aligned} &> G_s := \text{subs}\left(\left\{x = \frac{\text{Pi}}{4}, y = \frac{\text{Pi}}{4}, z = \frac{\text{Pi}}{4}\right\}, G\right) \\ &\quad G_s := \left(\frac{1}{2}\right) \bar{e}_x + \left(-\frac{1}{2}\right) \bar{e}_y + \bar{e}_z \end{aligned} \tag{22}$$

$$\begin{aligned} &> Q := \text{arrow}\left(\left\langle \frac{\text{Pi}}{4}, \frac{\text{Pi}}{4}, \frac{\text{Pi}}{4} \right\rangle, G_s, \text{shape} = \text{arrow}, \text{color} = \text{blue}\right) \\ &\quad Q := \text{PLOT3D}(\dots) \end{aligned} \tag{23}$$

$$> \text{display}(P, Q, \text{axes} = \text{boxed})$$



>